

## Answer Key

|       |   | Correct Option |                              |
|-------|---|----------------|------------------------------|
| Q. 1) | If the differential equation $(a \tan y + x) dx + (2x \sec^2 y - 3y) dy = 0$ is exact then the constant a is ...  | A              |                              |
|       | A) $a = 2$  |                | B) $a = 3$                   |
|       | C) $a = -2$   |                | D) $a = -3$                  |
| Q. 2) | If the differential equation $(y + \sin x) dx + (x - 2e^y) dy = 0$ is exact then the solution is .  | C              |                              |
|       | A) $xy + \cos x - 2e^y = c$   |                | B) $xy - \cos x - e^y = c$   |
|       | C) $xy - \cos x - 2e^y = c$   |                | D) $y^2 - \cos x - 2e^y = c$ |
| Q.3)  | The Integrating Factor for the differential equation $y(1 + 2xy)dx + x(1 - xy) dy = 0$ is ...   | A              |                              |
|       | A) $1/3x^2y^2$  |                | B) $3x^2y^2$                 |
|       | C) $1/y^2$  |                | D) $1/x^2$                   |
| Q. 4) | The Integrating Factor for the differential equation $(3xy^2 - y^3) dx - (2x^2y - xy^2) dy = 0$ is ...  | A              |                              |
|       | A) $1/x^2y^2$   |                | B) $x^2y^2$                  |
|       | C) $1/xy^2$   |                | D) $1/x^2y$                  |
| Q. 5) | The solution of the differential equation $\frac{dy}{dx} - \frac{y}{x} = x$ is ...  | D              |                              |
|       | A) $y + x^2 = xc$   |                | B) $xy - x^2 = c$            |
|       | C) $y - x = xc$   |                | D) $y - x^2 = xc$            |
| Q. 6  | The Integrating Factor for the differential equation $\frac{dy}{dx} + y \tan x = \sec x$ is ...   | A              |                              |
|       | A) $\sec x$   |                | B) $\cos x$                  |
|       | C) $\sin x$   |                | D) $\log \sec x$             |
| Q. 7  | Using Euler's method to solve the differential equation $\frac{dy}{dx} = 2 + \sqrt{xy}$ at $x=2$ in five steps with $y(1)=1$ taking $h = 0.2$ the approximate value of $y_2$ is | C              |                              |
|       | A) 1  |                | B) 1.6                       |
|       | C) 2.2771   |                | D) 3.0342                    |

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| Q. 8  | In Euler's modified method which of the following is true.   |  | B |
|       | A) $y_1^{(2)} = y_0 + h f(x_0, y_0)$   | B) $y_1^{(2)} = y_0 + \frac{h}{2} [f(x_0, y_0) + f(x_1, y_1^{(1)})]$ |   |
|       | C) $y_1^{(2)} = y_0 + \frac{h}{2} [f(x_0, y_0) + f(x_1, y_1^{(0)})]$   | D) $y_1^{(2)} = y_0 + \frac{h}{2} [f(x_0, y_0) - f(x_1, y_1^{(1)})]$ |   |
| Q. 9  | Using R-K method to solve the differential equation $dy/dx = 0.31 + 0.25y + 0.3x$ at $x=0.2$ with $h=0.2$ and $y(0)=0.72$ then the value of $k_2$ is .....                     |  | B |
|       | A) 0.980   | B) 0.1065  |   |
|       | C) 0.1067  | D) 1.1065  |   |
| Q. 10 | While solving the differential equation $dy/dx = y - xy$ with $y=2$ when $x=0$ by using Taylor's Series method then what is value $y'''_0$ .....                               |  | B |
|       | A) 4   | B) - 4   |   |
|       | C) 0   | D) - 3   |   |
| Q. 11 | Using Euler's modified method to solve the differential equation $\frac{dy}{dx} = x^2 + y$ at $x=0.1$ with $h=0.1$ and $y(0)=0.94$ the approximate value of $y_1^{(1)}$ is ... |  | D |
|       | A) 1.0395  | B) 0.0392  |   |
|       | C) 1.3209  | D) 1.0392  |   |
| Q. 12 | Find the approximated value of $x$ till third iterations for $x^3 - 5x + 1 = 0$ using Bisection Method. Where root lies in the interval( 0 , 1 )                               |  | A |
|       | A) 0.125   | B) 1.125   |   |
|       | C) 0.75  | D) 0.5   |   |
| Q. 13 | Find the approximated value of $x$ till second iterations for $x \log_{10} x = 1.2$ using Bisection Method. Where root lies in the interval ( 2 , 3 )                          |  | D |
|       | A) 2.25  | B) 2.5   |   |
|       | C) 0.75  | D) 2.75  |   |
| Q. 14 | Find the approximated value of $x_2$ using Secant Method for the equation $x^4 = 32$ where the root lies between 2 and 3   |  | B |
|       | A) 2.2425  | B) 2.2462  |   |
|       | C) 2.2546  | D) 2.5   |   |
| Q.15  | The equation $f(x)$ is given as $x e^x - 2 = 0$ . Considering the initial approximation at $x=0$ then by Newton Raphson method the value second approximation is ...           |  | B |
|       | A) 2   | B) 1.4236  |   |
|       | C) 1.035   | D) 1.0338  |   |
| Q.16  | The Iterative formula for Newton Raphson method is given by _____  |  | A |
|       | A) $x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$  | B) $x_n = x_{n+1} - \frac{f(x_n)}{f'(x_n)}$                          |   |
|       | C) $x_n = x_n + \frac{f(x_n)}{f'(x_n)}$  | D) $x_{n+1} = x_n + \frac{f(x_n)}{f'(x_{n+1})}$                      |   |

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| Q.17 | The value of $\int_0^{\infty} e^{-x^4} dx$ is                          |   | C |
|      | A) $\sqrt{\frac{1}{4}}$  | B) $\sqrt{\frac{3}{4}}$                                   |   |
|      | C) $\frac{1}{4} \sqrt{\frac{1}{4}}$                                    | D) $\sqrt{\frac{1}{2}}$                                   |   |
| Q.18 | The value of $\sqrt{\frac{15}{2}}$ is                                  |   | D |
|      | A) $\frac{13135}{16}$  | B) $\frac{3003\sqrt{\pi}}{128}$                           |   |
|      | C) $150150\sqrt{\pi}$  | D) $\frac{135135\sqrt{\pi}}{128}$                         |   |
| Q.19 | What is the value of $\beta\left(\frac{3}{2}, \frac{1}{2}\right)$ ?    |   | C |
|      | A) $\pi$   | B) $2\pi$   |   |
|      | C) $\pi/2$   | D) $\pi/4$  |   |
| Q.20 | What is the value of $\int_0^{\pi/2} \sqrt{\cot\theta} d\theta$        |   | C |
|      | A) $2\sqrt{\pi}$   | B) $\sqrt{\pi}/2$   |   |
|      | C) $\pi/\sqrt{2}$  | D) $\sqrt{2}/\pi$   |   |
| Q.21 | Which of the following is not true about Error function?               |   | A |
|      | A) $\operatorname{erf}(-x) = \operatorname{erf}(x)$                    | B) $\operatorname{erf}_c(-x) = 1 + \operatorname{erf}(x)$ |   |
|      | C) $\operatorname{erf}(x) - \operatorname{erf}_c(-x) = -1$             | D) $\operatorname{erf}(x) + \operatorname{erf}_c(x) = 1$  |   |
| Q.22 | The value of $\int_0^1 \int_0^1 \frac{1}{(1+x^2)(1+y^2)} dx dy$ is ... |   | C |
|      | A) $\pi^2/8$   | B) $\pi^2/4$  |   |
|      | C) $\pi^2/16$  | D) 0  |   |
| Q.23 | The value of $\int_0^2 \int_0^x xy dy dx$ is ....                      |   | A |
|      | A) 2   | B) $\frac{\pi}{2}$  |   |
|      | C) 16  | D) $\pi/16$   |   |
| Q.24 | The value of $\int_0^1 \int_0^y e^y dy dx$ is ....                     |   | C |
|      | A) 0   | B) e - 1  |   |
|      | C) 1   | D) 2  |   |
| Q.25 | The value of $\int_0^{\pi} \int_0^y \sin x dx dy$ is ....              |   | D |
|      | A) 0   | B) 1  |   |
|      | C) $\frac{\pi}{2}$   | D) $\frac{\pi}{2} - 1$                                    |   |